

FRACTIONAL KNAPSACK USING PYTHON.

Weights = [2, 3, 4, 5]
 Values = [10, 20, 30, 40]
 Capacity = 10

Step 1: Create a 2d array of (weights, value) in a list.

$l = [(2, 10), (3, 20), (4, 30), (5, 40)]$
 weight value

Step 2: Take ratio of either value/weight or weight/value and store them in a list.

If you are going for value/weight it will affect further steps accordingly,

$$x[i] = \frac{\text{value}}{\text{weight}} = \frac{2}{10} = 5.0$$

$$x = [5.0, 6.67, 7.5, 8]$$

Step 3: To map the ratios in descending order with respective weights and values, just initialize a variable with range of weights.

$$a = 4 \rightarrow [2, 3, 4, 5]$$

$$a = [0, 1, 2, 3]$$

Step 4: Map ratio in descending order using index.

$$a = [3, 2, 1, 0]$$

$$a = [3, 2, 1, 0]$$

Step 5: Check whether the capacity at index [i] is greater than provided capacity. If true then add the value of weight to maximum-value, to remove the weight from capacity which is equal to the value of weight added. i.e.

$$3 \rightarrow \text{Weight} = 5, \text{value} = 40$$

$$\rightarrow \text{Capacity}(10) > \text{weight}(5):$$

$$\therefore \text{maximum-value} = 40$$

$$\therefore \text{Capacity} = \text{capacity}(10) - \text{weight}(5)$$

$$\text{Capacity} = 5$$

$$2 \rightarrow \text{Weight} = 4, \text{value} = 30$$

$$\rightarrow \text{Capacity}(5) > \text{weight}(4)$$

$$\therefore \text{maximum-value} = 40 + 30 = 70$$

$$\therefore \text{Capacity} = \text{capacity}(5) - \text{weight}(4)$$

$$\text{Capacity} = 1$$

Step 6: Now if capacity is less than the weight in index (i) then add product of capacity and ratio of value/weight at index [i] i.e. to utilize total capacity provided.

$$1 \rightarrow \text{Weight} = 3, \text{value} = 20$$

$$\rightarrow \text{Capacity}(1) < \text{weight}(3)$$

$$\therefore \text{maximum-value} = \text{capacity}(1) \times \text{ratio of } v/w \text{ at index } [i] (6.67)$$

$$= 70 + 6.67 = 76.67$$